



Attempt the following questions.

**Question 1:****(05 pts)**

Consider the following code fragment:

```
for (i = 0; i < 1000; i++)
    column_sum[i] = 0.0;
    for (j = 0; j < 1000; j++)
        column_sum[i] += b[j][i];
```

- a) Identify the problem that causes poor memory system performance. (02 pts)  
 b) Make any reasonable assumption and restructure the code fragment to eliminate the problem. (03 pts)

**Question 2:****(05 pts)**

Formulate message passing costs in parallel computers in the following routing techniques:

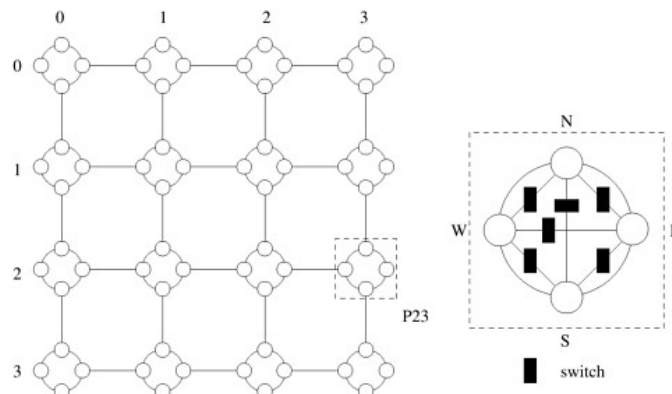
- a) Store-and-Forward Routing (01 pt)  
 b) Packet Routing (02 pts)  
 c) Cut-Through Routing (02 pts)

**Question 3:****(05 pts)**

- a) Consider a complete binary tree of  $2^d - 1$  nodes in which each node is a processing node. What is the minimum-dilation mapping of such a tree onto a d-dimensional hypercube? (03 pts)  
 b) Derive the diameter, number of links, and bisection width of a k-ary d-cube with p nodes. Define  $l_{av}$  to be the average distance between any two nodes in the network. Derive  $l_{av}$  for a k-ary d-cube. (02 pts)

**Question 4:****(05 pts)**

A  $\sqrt{P} \times \sqrt{P}$  reconfigurable mesh consists of a  $\sqrt{P} \times \sqrt{P}$  array of processing nodes connected to a grid-shaped reconfigurable broadcast bus. A  $4 \times 4$  reconfigurable mesh is shown. Each node has locally-controllable bus switches. The internal connections among the four ports, north (N), east (E), west (W), and south (S), of a node can be configured during the execution of an algorithm. Note that there are 15 connection patterns. For example, {SW, EN} represents the configuration in which port S is connected to port W and port N is connected to port E. Each bit of the bus carries one of 1-signal or 0-signal at any time. The switches allow the broadcast bus to be divided into subbuses, providing smaller reconfigurable meshes. For a given set of switch settings, a subbus is a maximally-connected subset of the nodes. Other than the buses and the switches, the reconfigurable mesh is similar to the standard two-dimensional mesh. Assume that only one node is allowed to broadcast on a subbus shared by multiple nodes at any time.



Determine **a)** the bisection width, **b)** the diameter, and **c)** the number of switching nodes and **d)** communication links for a reconfigurable mesh of  $\sqrt{P} \times \sqrt{P}$  processing nodes. What are **e)** the advantages and disadvantages of a reconfigurable mesh as compared to a wraparound mesh?

Good Luck  
 Dr. Islam ElShaarawy